Explain and justify mathematical ideas and decisions

Grade 8

Ministry of Education

Number represents,
describes, and
compares the
quantities of ratios,
rates, and percents.

fluency and flexibility extend to operations with fractions.

BIG IDEAS

Discrete linear relationships can be represented in many connected ways and used to identify and make generalizations. The relationship between surface area and volume of **3D objects** can be used to describe, measure, and compare spatial relationships.

Analyzing data by determining averages is one way to make sense of large data sets and enables us to compare and interpret.

Learning Standards

Curricular Competencies Content Students are expected to do the following: Students are expected to know the following: Reasoning and analyzing perfect squares and cubes Use logic and patterns to solve puzzles and play games square and cube roots • Use reasoning and logic to explore, analyze, and apply mathematical ideas percents less than 1 and greater than 100 (decimal • Estimate reasonably and fractional percents) numerical proportional reasoning (rates, ratio, Demonstrate and apply mental math strategies proportions, and percent) • Use tools or technology to explore and create patterns and relationships, and test operations with fractions (addition, subtraction, multiplication, division, and order of operations) Model mathematics in contextualized experiences discrete linear relations (extended to larger numbers, Understanding and solving limited to integers) Apply multiple strategies to solve problems in both abstract and contextualized expressions- writing and evaluating using substitution situations two-step equations with integer coefficients, constants, • Develop, demonstrate, and apply mathematical understanding through play, inquiry, and solutions and problem solving surface area and volume of regular solids, including · Visualize to explore mathematical concepts triangular and other right prisms and cylinders Engage in problem-solving experiences that are connected to place, story, cultural Pythagorean theorem practices, and perspectives relevant to local First Peoples communities, the local construction, views, and nets of 3D objects community, and other cultures central tendency Communicating and representing theoretical probability with two independent events • Use mathematical vocabulary and language to contribute to mathematical discussions financial literacy — best buys

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Area of Learning: MATHEMATICS

Grade 8

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Learning Standards (continued)

Curricular Competencies	Content
Communicate mathematical thinking in many ways	
 Represent mathematical ideas in concrete, pictorial, and symbolic forms 	
Connecting and reflecting	
Reflect on mathematical thinking	
 Connect mathematical concepts to each other and to other areas and personal interests 	
 Use mathematical arguments to support personal choices 	
 Incorporate First Peoples worldviews and perspectives to make connections to mathematical concepts 	

Big Ideas – Elaborations MATHEMATICS
Grade 8

numbers:

• Number: Number represents and describes quantity.

Sample questions to support inquiry with students:

- How can two quantities be compared, represented, and communicated?
- How are decimals, fractions, ratios, and percents interrelated?
- How does ratio use in mechanics differ from ratio use in architecture?

fluency:

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• Computational Fluency: Computational fluency develops from a strong sense of number.

Sample questions to support inquiry with students:

- When we are working with fractions, what is the relationship between addition and subtraction?
- When we are working with fractions, what is the relationship between multiplication and division?
- When we are working with fractions, what is the relationship between addition and multiplication?
- When we are working with fractions, what is the relationship between subtraction and division?

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Big Ideas – Elaborations MATHEMATICS
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Discrete linear relationships:

• Patterning: We use patterns to represent identified regularities and to make generalizations.

Sample questions to support inquiry with students:

- What is a discrete linear relationship?
- How can discrete linear relationships be represented?
- What factors can change a discrete linear relationship?

3D objects:

• Geometry and Measurement: We can describe, measure, and compare spatial relationships.

Sample questions to support inquiry with students:

- What is the relationship between the surface area and volume of regular solids?
- How can surface area and volume of regular solids be determined?
- How are the surface area and volume of regular solids related?
- How does surface area compare with volume in patterning and cubes?

data:

• Data and Probability: Analyzing data and chance enables us to compare and interpret.

Sample questions to support inquiry with students:

- · How does determining averages help us understand large data sets?
- What do central tendencies represent?
- How are central tendencies best used to describe a quality of a large data set?

Curricular Competencies – Elaborations

MATHEMATICS Grade 8

logic and patterns:

· including coding

reasoning and logic:

· making connections, using inductive and deductive reasoning, predicting, generalizing, drawing conclusions through experiences

Estimate reasonably:

• estimating using referents, approximation, and rounding strategies (e.g., the distance to the stop sign is approximately 1 km, the width of my finger is about 1 cm)

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Curricular Competencies – Elaborations

apply:

- extending whole-number strategies to decimals
- · working toward developing fluent and flexible thinking about number

Model:

• acting it out, using concrete materials (e.g., manipulatives), drawing pictures or diagrams, building, programming

multiple strategies:

• includes familiar, personal, and from other cultures

connected:

- in daily activities, local and traditional practices, the environment, popular media and news events, cross-curricular integration
- Patterns are important in First Peoples technology, architecture, and art.
- Have students pose and solve problems or ask questions connected to place, stories, and cultural practices.

Explain and justify:

· using mathematical arguments

Communicate:

• concretely, pictorially, symbolically, and by using spoken or written language to express, describe, explain, justify, and apply mathematical ideas; may use technology such as screencasting apps, digital photos

Reflect:

• sharing the mathematical thinking of self and others, including evaluating strategies and solutions, extending, and posing new problems and questions

other areas and personal interests:

• to develop a sense of how mathematics helps us understand ourselves and the world around us (e.g., cross-discipline, daily activities, local and traditional practices, the environment, popular media and news events, and social justice)

personal choices:

· including anticipating consequences

Incorporate First Peoples:

• Invite local First Peoples Elders and knowledge keepers to share their knowledge

make connections:

- Bishop's cultural practices: counting, measuring, locating, designing, playing, explaining (http://www.csus.edu/indiv/o/oreyd/ACP.htm_files/abishop.htm)
- www.aboriginaleducation.ca
- Teaching Mathematics in a First Nations Context, FNESC http://www.fnesc.ca/k-7/

Content – Elaborations

- perfect squares and cubes:using colour tiles, pictures, or multi-link cubes
 - building the number or using prime factorization

square and cube roots:

- finding the cube root of 125
- finding the square root of 16/169
- estimating the square root of 30

percents:

- A worker's salary increased 122% in three years. If her salary is now \$93,940, what was it originally?
- What is 1/2% of 1 billion?
- The population of Vancouver increased by 3.25%. What is the population if it was approximately 603,500 people last year?
- beading

proportional reasoning:

- two-term and three-term ratios, real-life examples and problems
- A string is cut into three pieces whose lengths form a ratio of 3:5:7. If the string was 105 cm long, how long are the pieces?
- creating a cedar drum box of proportions that use ratios to create differences in pitch and tone
- · paddle making

fractions:

- includes the use of brackets, but excludes exponents
- · using pattern blocks or Cuisenaire Rods
- simplifying $\frac{1}{2} \div \frac{9}{6} \times (7 \frac{4}{5})$
- drumming and song: 1/2, 1/4, 1/8, whole notes, dot bars, rests = one beat
- · changing tempos of traditional songs dependent on context of use
- · proportional sharing of harvests based on family size

discrete linear relations:

- · two-variable discrete linear relations
- expressions, table of values, and graphs
- scale values (e.g., tick marks on axis represent 5 units instead of 1)
- four quadrants, integral coordinates

expressions:

- using an expression to describe a relationship
- evaluating 0.5n 3n + 25, if n = 14

Content – Elaborations

- two-step equations:
 - modelling the preservation of equality (e.g., using a balance, manipulatives, algebra tiles, diagrams)
 - spirit canoe journey calculations

• solving and verifying 3x - 4 = -12

surface area and volume:

- · exploring strategies to determine the surface area and volume of a regular solid using objects, a net, 3D design software
- volume = area of the base x height
- surface area = sum of the areas of each side

Pythagorean theorem:

- modelling the Pythagorean theorem
- finding a missing side of a right triangle
- deriving the Pythagorean theorem
- · constructing canoe paths and landings given current on a river
- First Peoples constellations

3D objects:

- top, front, and side views of 3D objects
- matching a given net to the 3D object it represents
- drawing and interpreting top, front, and side views of 3D objects
- · constructing 3D objects with nets
- using design software to create 3D objects from nets
- · bentwood boxes, lidded baskets, packs

central tendency:

• mean, median, and mode

theoretical probability:

- with two independent events: sample space (e.g., using tree diagram, table, graphic organizer)
- rolling a 5 on a fair die and flipping a head on a fair coin is $1/6 \times 1/2 = 1/12$
- deciding whether a spinner in a game is fair

financial literacy:

- coupons, proportions, unit price, products and services
- proportional reasoning strategies (e.g., unit rate, equivalent fractions given prices and quantities)